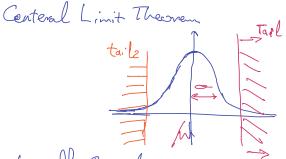
The Sun of indep. Random Variables



Chernoft Bound $P(X \ge (1+8) \text{ fm}) \le \left(\frac{e^8}{(1+8)^{(5+1)}}\right)$ $8 \ge 0 \qquad \qquad \leq e^{-8^2 \text{ fm}} / 3$

 $b(x < (1-8)h) < e_{-8} / (5)$

e.g.: given n indep. flip of Gins w/t p(head) = 0.5 what is the prob that you will See at Least 80% head? Using Markov Ineq. $P(X \ge t) \le \frac{h}{t}$ t = 0.8n, h = 0.5n $\Rightarrow P(X \ge 0.8n) \le \frac{5}{8}$

Using Chernoff Bound

Using Eq.(1) $P(X \ge (1+5) h)$ h = 0.5n (1+8).5n = .8n $\Rightarrow \delta = 8 - 1 = 0.6$ $P(X \ge (1+\delta) h) \leqslant e^{-5^2 h/3}$ $= e^{-(0.6)^{\frac{7}{3}} 0.5n}$ $= e^{-(0.6)^{\frac{7}{3}} 0.5n}$

e.9. N = 1000 $\frac{1}{e^{.06n}} < \frac{1}{e^{.60}}$

Team A in NBA wins every game with Prob D.75]

what is the Prob that team A hoses in more than 50% of the games $P(X \leq (1-8) \text{ m})$ h = 0.75 n

$$(1-8)h = (1-8).75n = .5n \Rightarrow \delta = 1-2/3 = 1/3$$
Using Eq.(2)
$$P(X \leq (1-8)h) \leq e^{-\frac{5^2h}{2}}$$

$$= e^{-\frac{5n}{36}}$$