CS401: Computer Algorithms I – Course Topics

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- Some representative problems
 - The stable matching problem
 - Five representative problems
- Basics of Algorithm Analysis (mostly review material)
 - Comptutational tractability
 - $\circ \ \ \, \text{Asymptotic order of growth}$
 - \circ Common running times
- Graphs (again, much review material)
 - Basic definitions and applications
 - Graph traversal
 - Testing bipartiteness
 - Connectivity in directed graphs
 - o DAGs and Topological ordering

• Greedy Algorithms

- Interval scheduling
- Scheduling to minimize lateness
- o Single-source shortest paths
- (Dijkstra's algorithm)
- Minimum spanning tree (Prim's
- algorithm, Kruskal's algorithm,
- UnionFind data structure)
- Clustering

• Divide and Conquer

Mergesort

• Solving recurrence relations using the following methods: Unrolling the recurrence, substitution (guess and check), and annihilators.

• Detour: Lower bound for

comparison-based sorting algorithms.

- Counting inversions
- Closest pair of points
- o Integer multiplication

• Dynamic Programming

- Weighted interval scheduling
- Coin changing
- o Segmented least squares
- Subset sum problem
- Sequence alignment
- Shortest paths

Network Flows

 $\circ~$ The Maximum-Flow problem and

Ford-Fulkerson algorithm

- Maximum flows and minimum cuts
- Improving Ford-Fulkerson by
- choosing good augmenting paths
- Bipartite matching
- Disjoint paths
- $\circ~$ Extensions to Max Flow
- Project selection

• Computational Intractability

• The complexity classes P, NP, EXP, and the importance of the P vs NP question

Polynomial-time reductions
(Hamiltonian Path, Vertex Cover,
Independent Set, Clique, Subset Sum)
A review of Turing Machines and
the Church-Turing Thesis

 $\circ~$ The Cook-Levin Theorem (SAT is NP-complete) and its proof

- \circ An introduction to the PCP theorem
- Independent learning via course project: Tractable special cases of NPhard problems
 - o Solving NP-hard problems on trees
 - Solving NP-hard problems on
 - graphs with bounded tree-width